

UK Cosmo Meeting
London, UK
March 12th, 2013

Preheating in Gauged M-flation around the Supersymmetric Vacuum and its Gravitational Wave Signatures

Amjad Ashoorioon (Lancaster University)

In collaboration with

Brandon Fung (Waterloo)

Robert B. Mann (Waterloo)

Marius Oltean (McGill)

Shahin Sheikh-Jabbari (IPM)

Based on a work in progress and

A.A., H. Firouzjahi, M.M. Sheikh-Jabbari JCAP 0906:018,2009, arXiv:0903.1481 [hep-th],

A.A., H. Firouzjahi, M.M. Sheikh-Jabbari JCAP 1005 (2010) 002, arXiv:0911.4284 [hep-th]

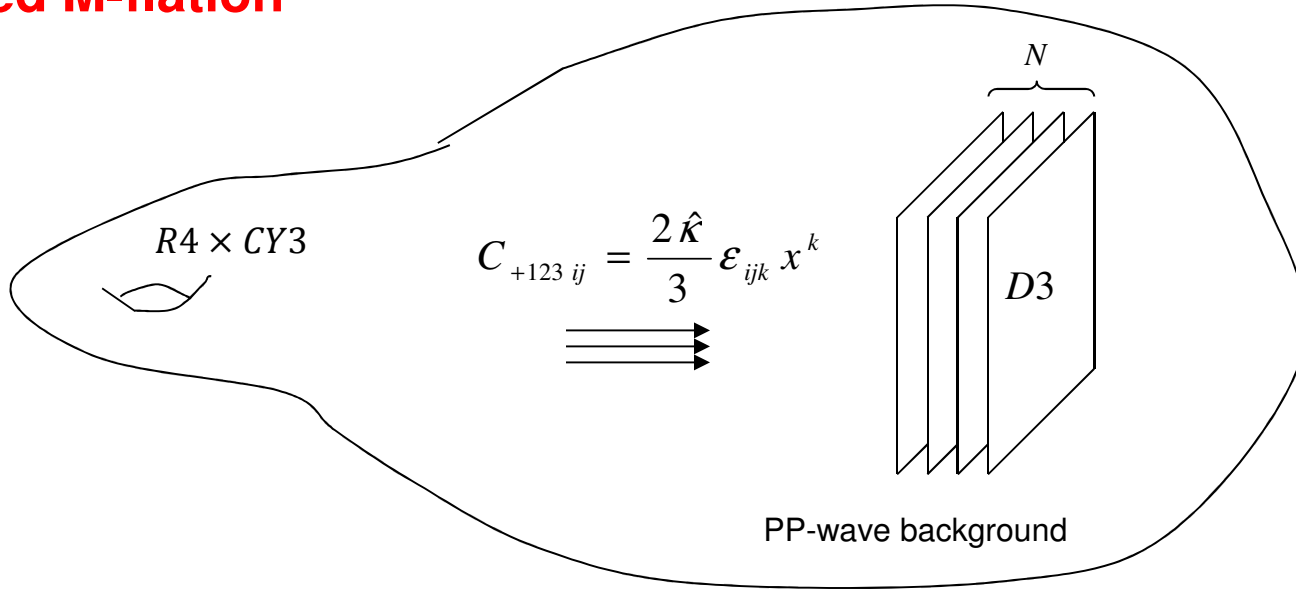
A.A., M.M. Sheikh-Jabbari, JCAP 1106 (2011) 014, arXiv:1101.0048 [hep-th]

A.A., U.Danielsson, M. M. Sheikh-Jabbari, Phys.Lett. B713 (2012) 353, arXiv:1112.2272 [hep-th]

Introduction

- ❑ Planck data strongly supports the idea of inflation as the theory of early universe and structure formation.
- ❑ The data reduces the lower bound on tensor/scalar ratio, r , to 0.11 (%95 *CL*) which puts some favourite models like $m^2\phi^2$ in trouble, considering Bunch-Davies vacuum. c.f. Ashoorioon, Dimopoulos, Sheikh-Jabbari & Shiu (2013)
- ❑ Still any detection of the gravity waves above $r \geq 0.01$ poses theoretical model-building challenges for inflationary scenarios:
 - To embed such a model in supergravity, one has to insure the flatness of the theory on scales beyond the limit of validity of the theory. Lyth (1997)
$$\frac{\Delta\phi}{M_{pl}} > 1.06 \left(\frac{r}{0.01}\right)^{1/2} \quad \text{c.f. Choudhury & Mazumdar (2013)}$$
 - In supergravity and stringy models of inflation, one usually finds the size of the region in which inflation can happen to be much smaller than M_{pl} McAllister & Baumann (2007)
- ❑ In this talk I will focus on a string theory motivated model of inflation that may solve this problem using **Matrices** as inflatons.
- ❑ The model has an embedded preheating mechanism in some regions which leads to the production of **high frequency gravitational waves**.

• Gauged M-flation



10-d IIB supergravity background

$$ds^2 = 2dx^+ dx^- - \hat{m}^2 \sum_{i=1}^3 (x^i)^2 (dx^+)^2 + \sum_{K=1}^8 dx_K dx_K$$

$i, j = 1, 2, 3$ parameterize 3 out of 6 dim \perp to the D3-branes and x^K denotes 3 spatial dim along and five transverse to the D3-branes.

$$S = \frac{1}{(2\pi)^3 l_s^4 g_s} \int d^4x \text{STr} \left(1 - \sqrt{-|g_{ab}|} \sqrt{|Q_J^I|} + \frac{i g_s}{4\pi l_s^2} [X^I, X^J] C_{IJ0123}^{(6)} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} \right)$$

Myers (1999)

$$g_{ab} = G_{MN} \partial_a X^M \partial_b X^N$$

$$M, N = 0, 1, \dots, 9$$

$$I, J = 4, 5, \dots, 9$$

$$a, b = 0, 1, 2, 3$$

$$Q^{IJ} = \delta^{IJ} + \frac{i}{2\pi l_s^2} [X^I, X^J]$$

Matrix Inflation from String Theory

With $\hat{m}^2 = \frac{4g_s^2 \hat{\kappa}^2}{9}$ the above background with constant dilaton is solution to the SUGRA

$$V = -\frac{1}{4(2\pi l_s^2)^2} [X_i, X_j][X_i, X_j] + \frac{ig_s \hat{\kappa}}{3 \cdot 2\pi l_s^2} \epsilon^{ijk} X_i [X_j, X_k] + \frac{1}{2} \hat{m}^2 X_i^2$$

Upon the field redefinition $\Phi_i \equiv \frac{X_i}{\sqrt{(2\pi)^3 g_s l_s^2}}$

$$V = \text{Tr} \left(-\frac{\lambda}{4} [\Phi_i, \Phi_j][\Phi_i, \Phi_j] + \frac{i\kappa}{3} \epsilon_{jkl} [\Phi_k, \Phi_l] \Phi_j + \frac{m^2}{2} \Phi_i^2 \right)$$

$$\lambda = 8\pi g_s \quad \kappa = \hat{\kappa} g_s \cdot \sqrt{8\pi g_s} \quad \hat{m}^2 = m^2$$

From the brane-theory perspective, it is necessary to choose \hat{m} and $\hat{\kappa}$ such that

$$\hat{m}^2 = \frac{4g_s^2 \hat{\kappa}^2}{9}$$

In the stringy picture, we have N D3-branes that are blown up into a **single giant D5-brane** under the influence of RR 6-form. The inflaton corresponds to the radius of this two sphere.

Truncation to the SU(2) Sector:

Φ_i are $N \times N$ matrices and therefore we have $3N^2$ scalars. It makes the analysis very difficult 🙄

Liam's talk

However from the specific form of the potential and since we have three Φ_i , it is possible to show that one can consistently restrict the classical dynamics to a sector with single scalar field:

$$\Phi_i = \hat{\phi}(t) J_i, \quad i = 1, 2, 3$$

J_i are N dim. irreducible representation of the SU(2) algebra:

$$[J_i, J_j] = i\epsilon_{ijk} J_k \quad \text{Tr}(J_i J_j) = \frac{N}{12} (N^2 - 1) \delta_{ij}$$

Plugging these to the action, we have:

$$S = \int d^4x \sqrt{-g} \left[\frac{M_P}{2} R + \text{Tr} J^2 \left(-\frac{1}{2} \partial_\mu \hat{\phi} \partial^\mu \hat{\phi} - \frac{\lambda}{2} \hat{\phi}^4 + \frac{2\kappa}{3} \hat{\phi}^3 - \frac{m^2}{2} \hat{\phi}^2 \right) \right] \quad \text{Tr}(J^2) \equiv \sum_{i=1}^3 \text{Tr}(J_i^2)$$

Defining $\phi \equiv (\text{Tr} J^2)^{1/2} \hat{\phi}$ to make the kinetic term canonical, the potential takes the form

$$V_0(\phi) = \frac{\lambda_{\text{eff}}}{4} \phi^4 - \frac{2\kappa_{\text{eff}}}{3} \phi^3 + \frac{m^2}{2} \phi^2 \quad \lambda_{\text{eff}} \equiv \frac{2\lambda}{\text{Tr} J^2} = \frac{8\lambda}{N(N^2-1)}, \quad \kappa_{\text{eff}} \equiv \frac{\kappa}{\sqrt{\text{Tr} J^2}} = \frac{2\kappa}{\sqrt{N(N^2-1)}}$$

Analysis of the Gauged M-flation around the Single-Block Vacuum

$$V(\phi) = \frac{\lambda_{\text{eff}}}{4} \phi^2 (\phi - \mu)^2 \quad \mu \equiv \frac{\sqrt{2}m}{\sqrt{\lambda_{\text{eff}}}}$$

Hill-top or Symmetry-Breaking inflation, Linde (1992)
Lyth & Bousso (2005)

In the stringy picture, we have N D3-branes that are blown up into a **giant D5-brane** under the influence of RR 6-form.

(a) $\phi_i > \mu$

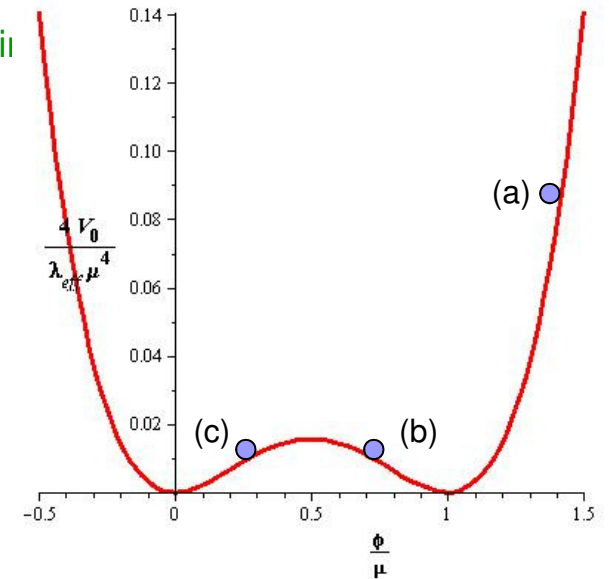
$$\begin{aligned} \phi_i &\approx 43.57 M_p & \phi_f &\approx 27.07 M_p & \mu &\approx 26 M_p \\ \lambda_{\text{eff}} &\approx 4.91 \times 10^{-14} & m &\approx 4.07 \times 10^6 M_p \end{aligned}$$

(b) $\mu/2 < \phi_i < \mu$

$$\begin{aligned} \phi_i &\approx 23.5 M_p & \phi_f &\approx 35.03 M_p & \mu &\approx 36 M_p \\ \lambda_{\text{eff}} &\approx 7.18 \times 10^{-14} & m &\approx 6.82 \times 10^6 M_p \end{aligned}$$

(c) $0 < \phi_i < \mu/2$

$$\begin{aligned} \phi_i &\approx 12.5 M_p & \phi_f &\approx .97 M_p & \mu &\approx 36 M_p \\ \lambda_{\text{eff}} &\approx 7.18 \times 10^{-14} & m &\approx 6.82 \times 10^6 M_p \end{aligned}$$



$$\begin{aligned} \lambda &\approx 1 \\ \downarrow \\ N &\approx 5 \times 10^4 \\ \downarrow \\ \Delta\phi &\leq 10^{-6} M_p \end{aligned}$$

Mass Spectrum of χ Spectators

(a) $(N-1)^2 - 1$ α -modes

$$l \in \mathbb{Z} \quad 0 \leq l \leq N-2$$

Degeneracy of each

l -mode is $2l + 1$

$$M_{\alpha,l}^2 = \frac{1}{2} \lambda_{\text{eff}} (l+2)(l+3)\phi^2 - 2\kappa_{\text{eff}} (l+2) + m^2$$

(b) $(N+1)^2 - 1$ β -modes

$$l \in \mathbb{Z} \quad 1 \leq l \leq N$$

Degeneracy of each

l -mode is $2l + 1$

$$M_{\beta,l}^2 = \frac{1}{2} \lambda_{\text{eff}} (l-2)(l-1)\phi^2 + 2\kappa_{\text{eff}} (l-1) + m^2$$

(c) $3N^2 - 1$ vector modes

$$M_{A,l}^2 = \frac{\lambda_{\text{eff}}}{4} \phi^2 l(l+1)$$

Degeneracy of each

l -mode is $2l + 1$

$$\left[(N-1)^2 - 1 \right] + \left[(N+1)^2 - 1 \right] + \left[3N^2 - 1 \right] = 5N^2 - 1$$

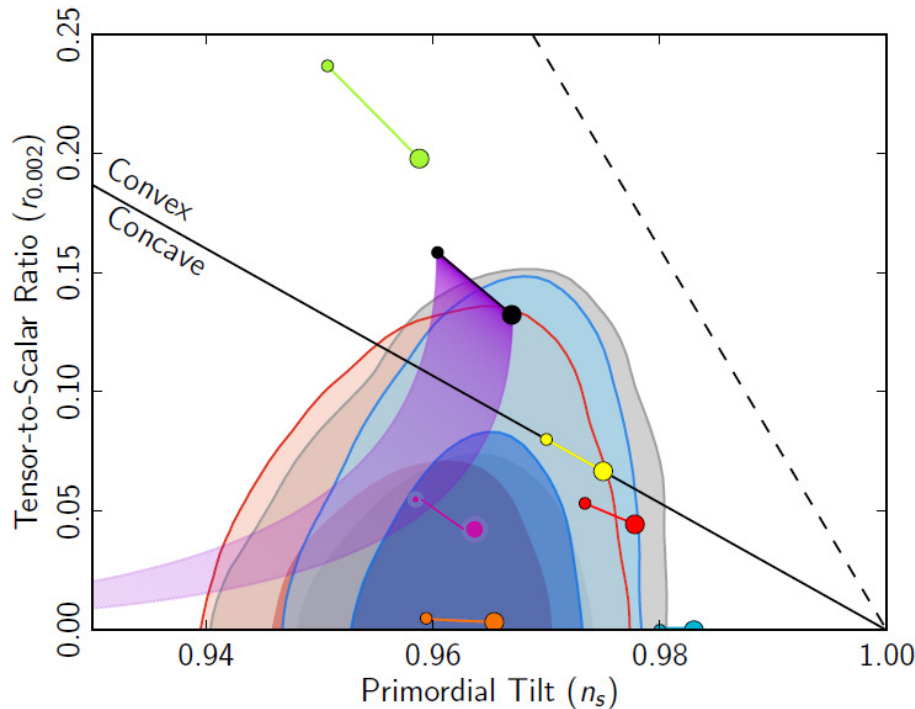
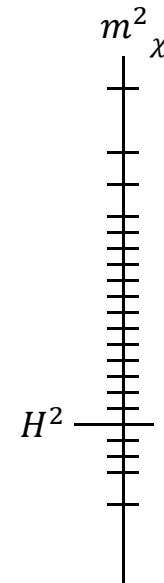
α -modes β -modes vector-field modes

C) Power Spectra in Symmetry-Breaking Inflation $0 < \phi < \mu/2$

$$\lambda_{\text{eff}} \approx 7.187 \times 10^{-14} \quad \& \quad \mu \approx 36 M_P \implies n_{\mathcal{R}} \approx 0.961 \quad \& \quad P_{\mathcal{R}} \approx 2 \times 10^{-9}$$

$l = 1$	$6\lambda_{\text{eff}}\phi^2 -$	1.23		
α	$6\kappa_{\text{eff}}\phi$	$\times 10^{-11}$	0.953	3
	$+ m^2$			

$$\frac{P_{S_{\alpha,1}}}{P_R} = 5.12 \times 10^{-3}$$



- Planck+WP
- Planck+WP+highL
- Planck+WP+BAO
- Natural Inflation
- - Power law inflation
- Low Scale SSB SUSY
- R^2 Inflation
- $V \propto \phi^{2/3}$
- $V \propto \phi$
- $V \propto \phi^2$
- $V \propto \phi^3$
- $N_* = 50$
- $N_* = 60$
- Gauged M-flation

Liam McAllister talk

$$r \approx 0.048$$

$$n_T \approx -0.006$$

CMBPOL or QUIET should be able to verify this scenario.

Particle Creation and Preheating Scenario around SUSY Vacuum

The backreaction of the spectator modes on the inflaton dynamics can become large when $\varepsilon, \eta \approx 1$

- This could be the bonus of our model, as spectator modes help to drain the energy of the inflaton, since their masses change very fast.
- One can show that if inflation ends in the susy-breaking vacuum, this process is not effective to produce spectator particles through parametric resonance:

$$M_{\alpha,\beta}^2 \Big|_{\phi=\mu} = \frac{\lambda_{\text{eff}} \mu^2}{2} (\omega+1)^2 \quad \begin{matrix} \omega_\alpha = -(l+2) \\ \omega_\beta = (l-1) \end{matrix} \quad M_A^2 \Big|_{\phi=\mu} = \frac{\lambda_{\text{eff}} \mu^2}{4} l(l+1)$$

rest masses are large around susy-breaking vacuum.

- For α and β modes: $\ddot{\chi} + 3H\dot{\chi} + \Omega_k^2 \chi = 0$
- For the gauge mode $\ddot{A} + H\dot{A} + \Omega_k^2 A = 0$

for example for α and β modes:

$$\Omega_k^2 = \frac{k^2}{a^2} + M_\chi^2 + g_3 \varphi + g_4 \varphi^2 \quad \varphi \equiv \phi - \mu \quad g_4^2 = \frac{\lambda_{\text{eff}} (\omega^2 - \omega)}{2} \quad g_3 = \frac{\lambda_{\text{eff}} \mu}{2} (2\omega^2 + \omega)$$

$$\forall \omega, \quad \frac{\dot{\Omega}_k}{\Omega_k^2} \Big|_{\phi \approx \mu} \ll 1 \implies$$

No parametric resonance around the susy-breaking vacuum

Particle Creation and Preheating Scenario around SUSY Vacuum

- The situation is quite different around the SUSY vacuum

$$M_{\alpha,\beta}^2 \Big|_{\phi=0} = \frac{\lambda_{\text{eff}} \mu^2}{2}$$

$$M_A^2 \Big|_{\phi=0} = 0$$

- For large values of ω for α and β modes and for all values of l for the gauge modes

$$\frac{\dot{\Omega}_k}{\Omega_k^2} \Big|_{\phi \approx 0} \gg 1 \quad \longrightarrow \quad \text{parametric resonance happens.}$$

- $X_\ell = a^{3/2} \chi_\ell$ & $\mathcal{A}_\ell = a^{1/2} A_\ell$ & $t' \equiv \mu \sqrt{\frac{\lambda_{\text{eff}}}{2}} t$ & $' \equiv \frac{d}{dt'}$ & $\ell^2 \equiv \frac{2k^2}{\lambda_{\text{eff}} \mu^2}$

$$X_\ell'' + \Omega_\omega^2 X_\ell + \frac{2qX_\ell^3}{a^3 \mu^2} = 0$$

$$\mathcal{A}_\ell'' + \Omega_l^2 \mathcal{A}_\ell = 0$$

$$\Omega_\omega^2 \equiv \frac{\ell^2}{a^2} + \frac{\varphi^2}{\mu^2} (\omega^2 - \omega) + \frac{3\varphi\omega}{\mu} + 1 - \frac{3a'^2}{4a^2} - \frac{3a''}{2a}$$

$$\Omega_l^2 \equiv \frac{\ell^2}{a^2} + \frac{\varphi^2}{2\mu^2} (l^2 + l) + \frac{1}{4} \frac{a'^2}{a^2} - \frac{a''}{2a}$$

$$\lim_{t' \rightarrow 0} X_\ell = \frac{\exp(-i\Omega_\omega t')}{\sqrt{2\Omega_\omega}}$$

$$\lim_{t' \rightarrow 0} \mathcal{A}_\ell = \frac{\exp(-i\Omega_l t')}{\sqrt{2\Omega_l}}$$

$$n_\ell^\omega = \frac{\Omega_\omega}{2} \left(\frac{\mu^2 \lambda}{2} \frac{|X_\ell'|^2}{\Omega_\omega^2} + |X_\ell|^2 \right) - \frac{1}{2}$$

$$n_\ell^l = \left(\frac{\Omega_l}{2} \left(\frac{\mu^2 \lambda}{2} \frac{|\mathcal{A}_\ell'|^2}{\Omega_l^2} + |\mathcal{A}_\ell|^2 \right) - \frac{1}{2} \right) \frac{1}{a^2}$$

GW production from Preheating

- Parametric resonance at the end of inflation could be a source of gravitational waves.
- Parametric resonance leads to exponential particle production for some specific momenta in Fourier space, which leads to **large inhomogeneities** in the energy density of the universe.

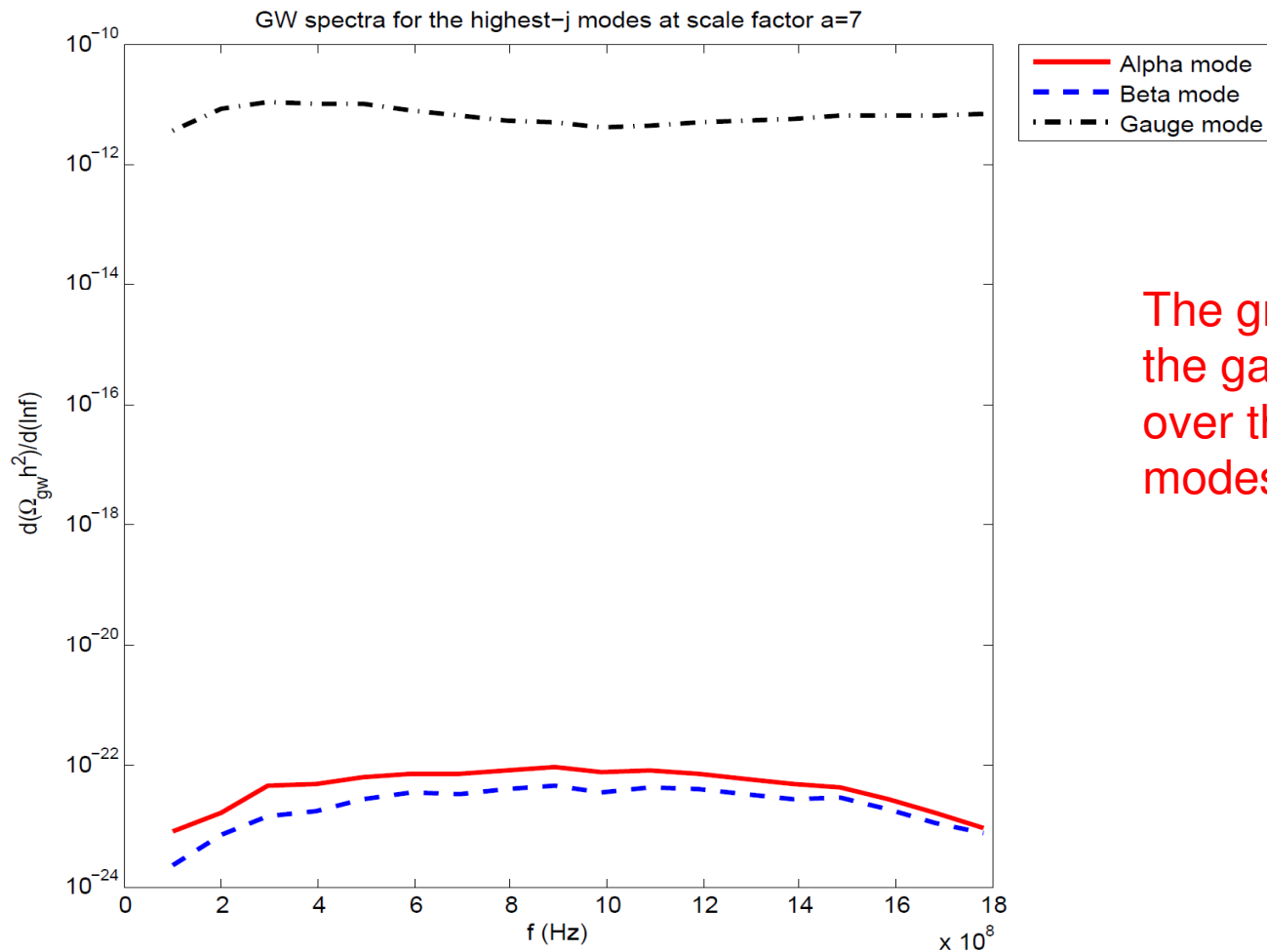
$$\ddot{h}_{ij} - 2\left(\frac{\dot{a}^2}{a^2} + 2\frac{\ddot{a}}{a}\right)h_{ij} + 3\frac{\dot{a}}{a}\dot{h}_{ij} - \frac{1}{a}\nabla^2 h_{ij} = \frac{16\pi G}{a^2}\delta S_{ij}^{TT} \quad \text{where} \quad \delta S_{ij} = \delta T_{ij} - \frac{\delta_{ij}}{3}T_k^k$$

$$\frac{d\Omega_{GW}}{d \ln k} = \frac{1}{\rho_{crit}} \frac{d\rho}{d \ln k} = \frac{\pi k^3}{3H^2 L^2} \sum_{i,j} |h_{ij,0}(k)|^2$$

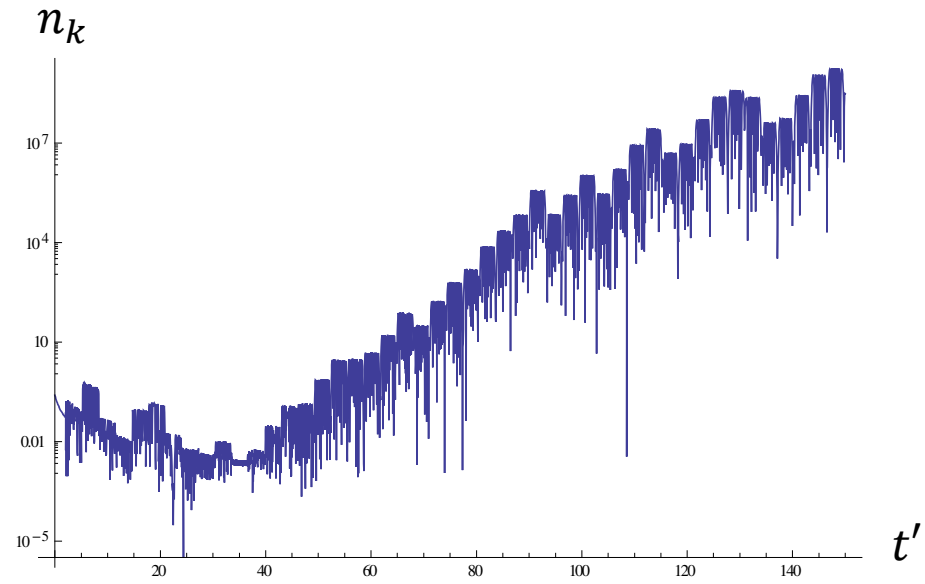
- This is in addition to the stochastic background of GW produced during inflation which probes the inflationary potential 60 e-folds before the end of inflation.
- Since the universe is transparent to gravitational radiation during its history, they can be a useful source of information from early universe.

GW production from Preheating: Single Mode

- We used HLattice (developed by [Zhiqi Huang \(2007\)](#)) to compute the GW spectrum produced by individual highest j modes as the preheat field

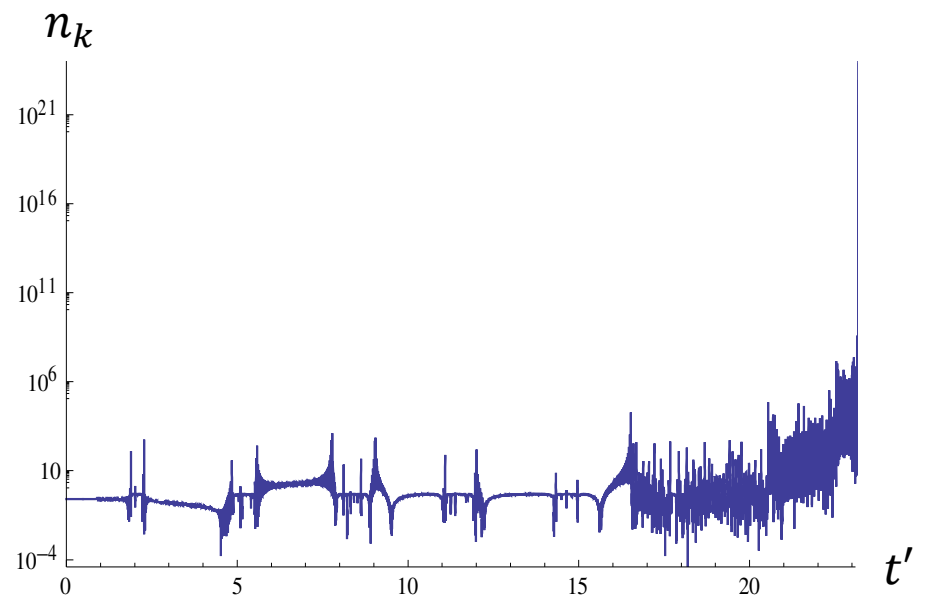


The gravitational wave from the gauge modes dominates over the ones from α and β modes.



Largest j Gauge modes

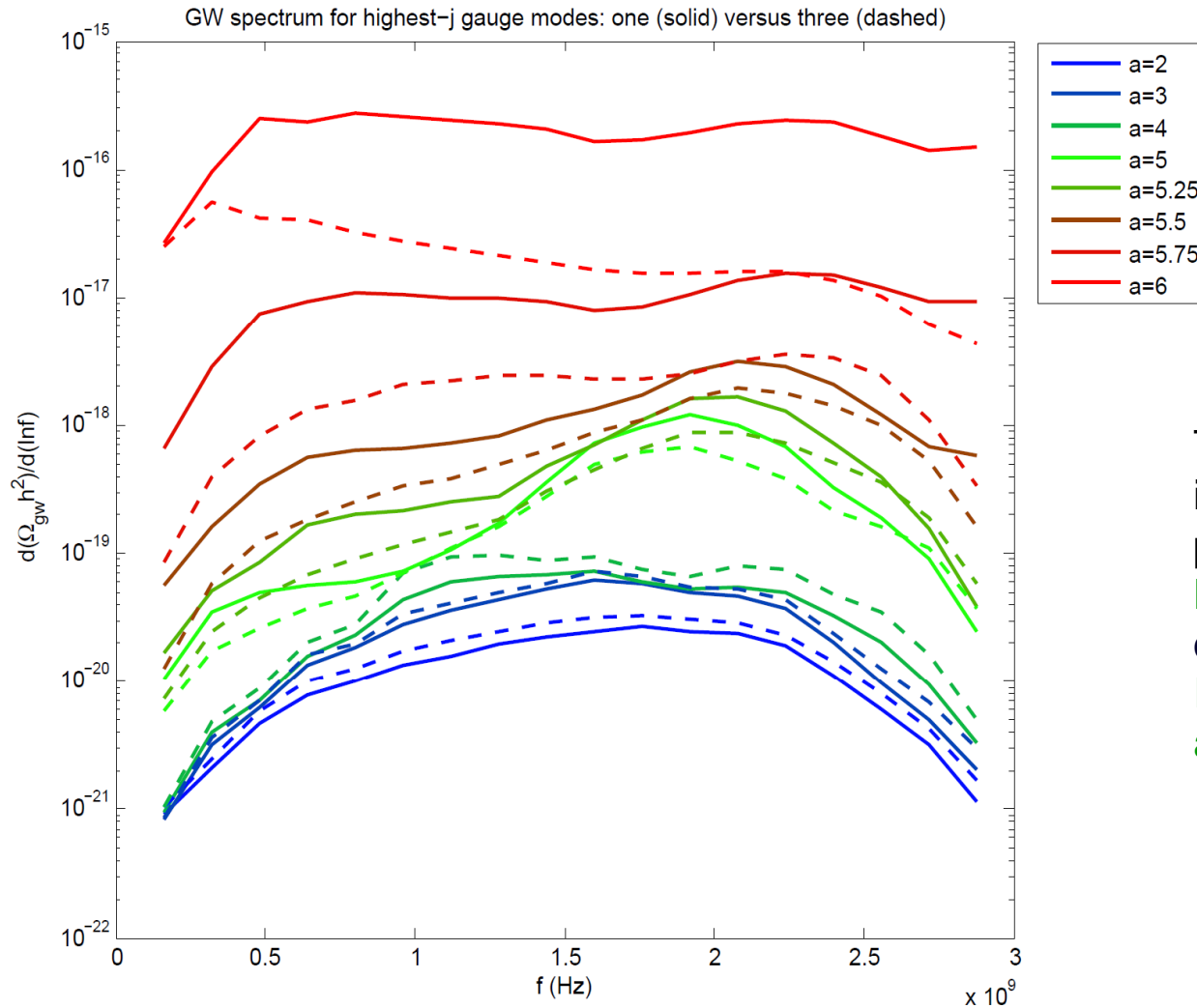
$$\ell = 0$$



Largest j beta mode

$$\ell = 0$$

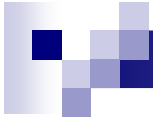
GW production from Preheating: Three largest j Gauge Mode



The signal may be seen in HFGW detectors that probe the GHz band
Birmingham HFGW detector
or
INFN Genoa HFGW resonant antenna

Conclusions

- M-flation can solve the **fine-tunings** associated **with chaotic inflation** couplings and produce **super-Planckian effective field excursions** during inflation.
- M-flation which is qualitatively **new third venue** within string theory inflationary model-building using the internal matrix degrees of freedom. the first two being open string and closed string models
- Due to Matrix nature of the fields there would be many scalar fields in the model. This leads to the production of **isocurvature productions** at the CMB scales.
- Due to **hierarchical mass structure** of the isocurvature modes, one can avoid the **“beyond-the-cutoff”** problem, even if the cutoff is reduced by the presence of the species.
A.A., M.M. Sheikh-Jabbari, JCAP 1106 (2011) 014, arXiv:1101.0048 [hep-th]
- The loop corrections from the interactions of the graviton with the scalar field create the **quadratically divergent**, $\frac{\Lambda^2}{M_p^2} R$ conformal mass type term which leads to the problem, if the **UV cutoff** of the theory is of order **Planck mass**. In M-flation such an induced term is naturally suppressed.
A.A., U.Danielsson, M. M. Sheikh-Jabbari, Phys.Lett. B713 (2012) 353, arXiv:1112.2272 [hep-th]
- M-flation has a natural **built-in mechanism of preheating** to end inflation around the SUSY vacuum. The parametric resonance produces large **GHz frequency** gravitational wave spectrum which could be seen by ultra-high frequency gravitational probes.



Thank you